Warm-Ups [9/22/08]

1. Given $x=1$ and $y=1$, we have

$$
\begin{aligned}
& x=y \\
& x^{2}=x y \\
& x^{2}-y^{2}=x y-y^{2} \\
& (x+y)(x-y)=y(x-y) \\
& x+y=y
\end{aligned}
$$

Substituting the given values

$$
\begin{array}{r}
1+1=1 \\
2=1
\end{array}
$$

What is wrong with this proof?
2. My daughter is twice as old as my son and half as old as I am. In twenty-two years my son will be half my age. How old is my daughter?
3. How many zeros are there at the end of the quantity "100!" ?

